

1) KCL: current down 150Ω : $i_{50} = +100 - 200 = -100\text{ mA}$

KVL: $V_{ab} = 0.1 \times 150 + 0.2R = 15 + 20 = 35\text{ V}$ $V_{Th} = V_{ab} = 35\text{ V}$

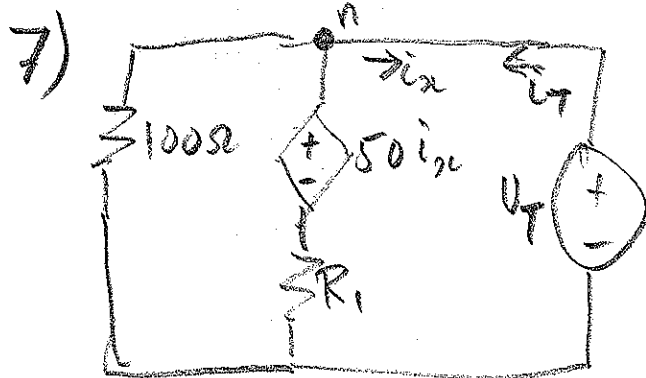
2) short-circuit a-b, $i_{sc} = 200 - \frac{150}{R+150} \cdot 100 = 140\text{ mA}$, $i_N = i_{sc} = 140\text{ mA}$

3) Remove redundant resistances of 2Ω , 3Ω , and 40Ω .
 source transformation $V_s/5\Omega \rightarrow 1\text{ A}/5\Omega$, combine $1\text{ A}/5\Omega$ and $-1\text{ A}/20\Omega$ to $0\text{ A}/4\Omega \Rightarrow 0\text{ V}/4\Omega$, combine with $-20\text{ V} \Rightarrow V_{Th} = -20\text{ V}$

4) From 3) $R_{eq} = 4\Omega$, $R_{Th} = 4\Omega + R_1 = 6\Omega$

5) $-0.01 + \frac{V_{ab}}{100} + \frac{V_{ab}}{R_1} = 0 \Rightarrow \frac{V_{ab}}{50} = 0.01 \Rightarrow V_{ab} = 0.5 \Rightarrow V_{Th} = 0.5\text{ V}$

6) require $V_{ab}'' = 0.5\text{ V}$, $\frac{-100}{100+R_1} V_2 = -0.5 \Rightarrow V_2 = 0.5 \frac{200}{100} = 1.0\text{ V}$



KCL at n: $\frac{V_T}{100} + \frac{V_T - 50i_x}{R_1} - i_T = 0$

$i_x = -i_T \Rightarrow$

$V_T + V_T + 50i_T - 100i_T = 0$

$2V_T = 50i_T \Rightarrow R_{Th} = \frac{V_T}{i_T} = 25\Omega$

8) $V_p = i_s R_3$, $i_2 = \frac{V_n}{R_2} = \frac{i_s R_3}{R_2} = i_s$, $i_1 = 2i_s$, $V_o = 2i_s R_1 + i_s R_3$

$1 = i_s (10 + 10) \Rightarrow i_s = 0.05\text{ mA}$

9) $V_1 = -V_s$, $V_2 = -V_s - 2i_s R = -3V_s$, $V_o = -3V_s - 5i_s R = -8V_s$
 $V_s = \frac{-V_o}{8} = 1$, $P_s = V_s^2 / R = \frac{1}{500} = 2\text{ mW}$

10) $V_2 = -\frac{R_2}{R_1} V_1 = -0.4\text{ V}$, $i_4 = \frac{V_2}{R_4} = \frac{-0.4}{10}$, $V_o = -i_4 R_3 = -\frac{-0.4}{10} \times 50 = 2\text{ V}$

11) $L_{eq} = ((2L // L) + L) // L + 2L = \frac{21}{8} L = \frac{21}{8}\text{ H}$

$i(t) = \frac{1}{L} \int v(t) dt = \frac{8}{21} \int 4 \cos 3t dt = \frac{32}{63} \sin 3t = 507.9 \sin 3t\text{ mA}$

12) $i_1(t) = C_1 \frac{d v(t)}{dt} = \frac{C_1}{C_1 + C_2} \frac{d}{dt} \left[\int i(t) dt + i(0) \right] = \frac{C_1}{C_1 + C_2} i(t) = te^{-t}$

$$13) C_{eq1} = 4 + 12 = 16 \text{ F}, C_{eq2} = \frac{1}{2} \times 16 \text{ F} = 8 \text{ F}, C_{eq3} = 8 + C, \\ C_{eq4} = C + 8 + 12 = 20 + C, \frac{1}{7.5} = \frac{1}{10} + \frac{1}{20+C} \Rightarrow \frac{2.5}{75} = \frac{1}{20+C} \Rightarrow C = 10 \text{ F}$$

$$14) v_1 = (0.05 - 0.005) \frac{di}{dt}, v = (0.05 - 0.005 + 0.01 - 0.005) \frac{di}{dt} \\ v_1/v = \frac{0.045}{0.05} = 0.9$$

$$15) \tau = \frac{L}{R_{eq}} = \frac{0.2}{\frac{2}{3}R} = \frac{0.3}{50} = 6 \text{ ms}$$

$$16) i_2(0^+) = \frac{100}{100 + 2R} \cdot 1.5 = 0.75 \text{ A}, v(0^+) = -i_2(0^+) R_{eq} = \\ -0.75 \times \frac{2}{3}R = -25 \text{ V}$$

$$17) v_c(0^+) = \frac{R_2}{R_1 + R_2 + 4} \times 24 = 8 \text{ V}, v_c(\infty) = 12 \text{ V}, \tau = R_{eq}C = (4/14)C = \\ 2 \text{ s}, v_c(t) = 12 - 4e^{-t/2}, v_c(0.5) = 12 - 4e^{-0.5} \approx 8.88 \text{ V}, \\ W_c = \frac{1}{2} CV^2 \approx \frac{1}{2} 8.88^2 \approx 39.47 \text{ J}$$

$$18) v_c(0^+) = 0, v_c(\infty) = 1 \times 2 = 2 \text{ V}, \tau = 10^{-6} \times 2 \times 10^3 = 2 \text{ ms} \\ v_c(t) = 2 - 2e^{-500t} \text{ V}, v_{cmax} = v_c(0.001) = 2 - 2e^{-1/2} \approx \\ 0.79 \text{ V}$$

$$19) w_{tot} = \int_0^{1 \text{ ms}} p(t) dt = \int_0^{1 \text{ ms}} 10^{-3} \times (2 - 2e^{-500t}) dt = 2 \mu\text{J} - 2 \times 10^{-3} \int_0^{1 \text{ ms}} e^{-500t} dt = \\ 2 \mu\text{J} - \frac{2 \times 10^{-3}}{-500} e^{-500t} \Big|_0^{1 \text{ ms}} = 2 \mu\text{J} + 4 \times 10^{-6} (e^{-1/2} - 1) \approx 0.43 \mu\text{J}$$

$$20) i(0^+) = \frac{12}{3} = \frac{4}{3} \text{ A}, i(\infty) = \frac{2i_a}{3}, i_a = \frac{2i_a - 12}{6} = \frac{i_a}{3} - 2 \Rightarrow \frac{2}{3}i_a = 2 \\ i_a = 3 \text{ A} \Rightarrow i(\infty) = -2 \text{ A}, \text{ find } R_{Th}: i_a = \frac{2i_a}{6} \Rightarrow i_a = 0 \Rightarrow R_{Th} = 3 \Omega \\ i(t) = -2 + (\frac{4}{3} + 2)e^{-t/\tau} = -2 + \frac{10}{3}e^{-t/6} \\ i(0.2) = -2 + \frac{10}{3}e^{-0.1} = 1.016 \text{ A}$$